



National  
Qualifications  
2017

**X747/76/11**

**Mathematics  
Paper 1  
(Non-Calculator)**

FRIDAY, 5 MAY

9:00 AM – 10:10 AM

**Total marks — 60**

Attempt ALL questions.

**You may NOT use a calculator.**

Full credit will be given only to solutions which contain appropriate working.

State the units for your answer where appropriate.

Answers obtained by readings from scale drawings will not receive any credit.

Write your answers clearly in the spaces provided in the answer booklet. The size of the space provided for an answer should not be taken as an indication of how much to write. It is not necessary to use all the space.

Additional space for answers is provided at the end of the answer booklet. If you use this space **you must clearly identify the question number** you are attempting.

Use **blue** or **black** ink.

Before leaving the examination room you must give your answer booklet to the Invigilator; if you do not, you may lose all the marks for this paper.



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## FORMULAE LIST

### Circle:

The equation  $x^2 + y^2 + 2gx + 2fy + c = 0$  represents a circle centre  $(-g, -f)$  and radius  $\sqrt{g^2 + f^2 - c}$ .

The equation  $(x - a)^2 + (y - b)^2 = r^2$  represents a circle centre  $(a, b)$  and radius  $r$ .

### Scalar Product:

$\mathbf{a} \cdot \mathbf{b} = |\mathbf{a}| |\mathbf{b}| \cos \theta$ , where  $\theta$  is the angle between  $\mathbf{a}$  and  $\mathbf{b}$

or  $\mathbf{a} \cdot \mathbf{b} = a_1 b_1 + a_2 b_2 + a_3 b_3$  where  $\mathbf{a} = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix}$  and  $\mathbf{b} = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$ .

### Trigonometric formulae:

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\sin 2A = 2 \sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A$$

$$= 2 \cos^2 A - 1$$

$$= 1 - 2 \sin^2 A$$

### Table of standard derivatives:

$f(x)$	$f'(x)$
$\sin ax$	$a \cos ax$
$\cos ax$	$-a \sin ax$

### Table of standard integrals:

$f(x)$	$\int f(x) dx$
$\sin ax$	$-\frac{1}{a} \cos ax + c$
$\cos ax$	$\frac{1}{a} \sin ax + c$

ATTEMPT ALL QUESTIONS

MARKS

Total marks — 60

1. Functions  $f$  and  $g$  are defined on suitable domains by  $f(x) = 5x$  and  $g(x) = 2 \cos x$ .
- (a) Evaluate  $f(g(0))$ . 1
- (b) Find an expression for  $g(f(x))$ . 2

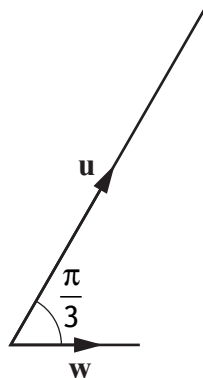
2. The point  $P(-2, 1)$  lies on the circle  $x^2 + y^2 - 8x - 6y - 15 = 0$ .  
Find the equation of the tangent to the circle at  $P$ . 4

3. Given  $y = (4x - 1)^{12}$ , find  $\frac{dy}{dx}$ . 2

4. Find the value of  $k$  for which the equation  $x^2 + 4x + (k - 5) = 0$  has equal roots. 3

5. Vectors  $\mathbf{u}$  and  $\mathbf{v}$  are  $\begin{pmatrix} 5 \\ 1 \\ -1 \end{pmatrix}$  and  $\begin{pmatrix} 3 \\ -8 \\ 6 \end{pmatrix}$  respectively.

- (a) Evaluate  $\mathbf{u} \cdot \mathbf{v}$ . 1
- (b)

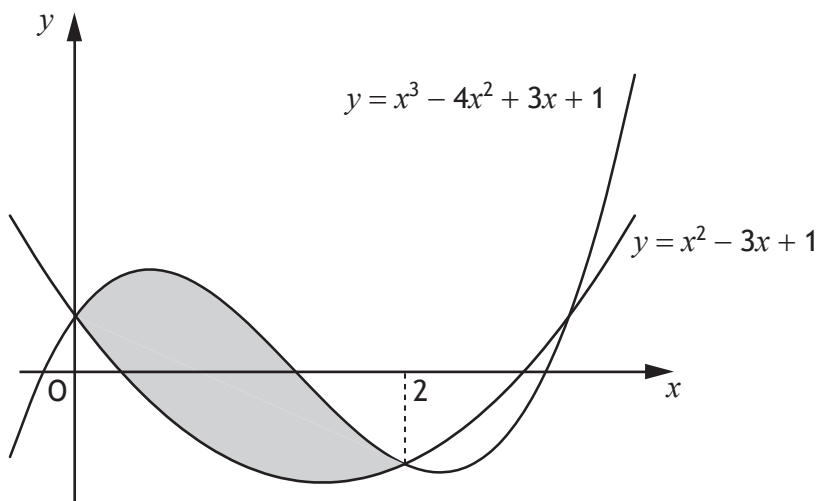


Vector  $\mathbf{w}$  makes an angle of  $\frac{\pi}{3}$  with  $\mathbf{u}$  and  $|\mathbf{w}| = \sqrt{3}$ .

- Calculate  $\mathbf{u} \cdot \mathbf{w}$ . 3

6. A function,  $h$ , is defined by  $h(x) = x^3 + 7$ , where  $x \in \mathbb{R}$ .  
Determine an expression for  $h^{-1}(x)$ . 3
7. A(-3, 5), B(7, 9) and C(2, 11) are the vertices of a triangle.  
Find the equation of the median through C. 3
8. Calculate the rate of change of  $d(t) = \frac{1}{2t}$ ,  $t \neq 0$ , when  $t = 5$ . 3
9. A sequence is generated by the recurrence relation  $u_{n+1} = m u_n + 6$  where  $m$  is a constant.
- (a) Given  $u_1 = 28$  and  $u_2 = 13$ , find the value of  $m$ . 2
- (b) (i) Explain why this sequence approaches a limit as  $n \rightarrow \infty$ . 1
- (ii) Calculate this limit. 2

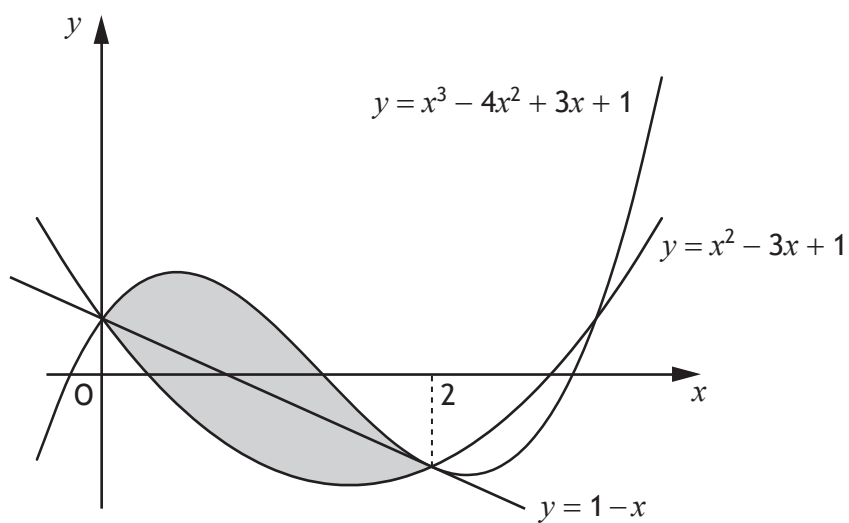
10. Two curves with equations  $y = x^3 - 4x^2 + 3x + 1$  and  $y = x^2 - 3x + 1$  intersect as shown in the diagram.



- (a) Calculate the shaded area.

5

The line passing through the points of intersection of the curves has equation  $y = 1 - x$ .



- (b) Determine the fraction of the shaded area which lies below the line  $y = 1 - x$ .

4

[Turn over

11. A and B are the points  $(-7, 2)$  and  $(5, a)$ .  
AB is parallel to the line with equation  $3y - 2x = 4$ .  
Determine the value of  $a$ . 3
12. Given that  $\log_a 36 - \log_a 4 = \frac{1}{2}$ , find the value of  $a$ . 3
13. Find  $\int \frac{1}{(5-4x)^{\frac{1}{2}}} dx$ ,  $x < \frac{5}{4}$ . 4
14. (a) Express  $\sqrt{3} \sin x^\circ - \cos x^\circ$  in the form  $k \sin(x-a)^\circ$ ,  
where  $k > 0$  and  $0 < a < 360$ . 4
- (b) Hence, or otherwise, sketch the graph with equation  
 $y = \sqrt{3} \sin x^\circ - \cos x^\circ$ ,  $0 \leq x \leq 360$ . 3
- Use the diagram provided in the answer booklet.

15. A quadratic function,  $f$ , is defined on  $\mathbb{R}$ , the set of real numbers.

Diagram 1 shows part of the graph with equation  $y = f(x)$ .

The turning point is  $(2, 3)$ .

Diagram 2 shows part of the graph with equation  $y = h(x)$ .

The turning point is  $(7, 6)$ .

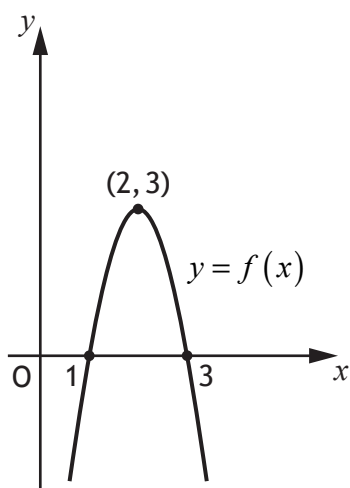


Diagram 1

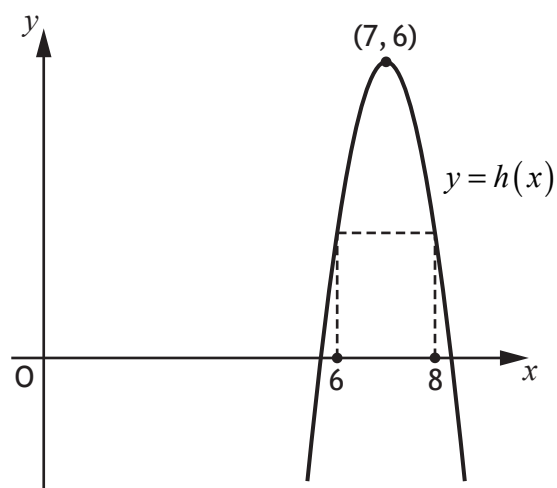


Diagram 2

(a) Given that  $h(x) = f(x + a) + b$ .

Write down the values of  $a$  and  $b$ .

2

(b) It is known that  $\int_1^3 f(x) dx = 4$ .

Determine the value of  $\int_6^8 h(x) dx$ .

1

(c) Given  $f'(1) = 6$ , state the value of  $h'(8)$ .

1

[END OF QUESTION PAPER]

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National  
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2017

Mark

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**X747/76/01**

**Mathematics Paper 1 (Non-Calculator)  
Answer Booklet**

FRIDAY, 5 MAY

9:00 AM – 10:10 AM



\* X 7 4 7 7 6 0 1 \*

Fill in these boxes and read what is printed below.

Full name of centre

--

Town

--

Forename(s)

--

Surname

--

Number of seat

--

Date of birth

Day

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Month

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Year

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Scottish candidate number

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Write your answers clearly in the spaces provided in this booklet. The size of the space provided for an answer should not be taken as an indication of how much to write. It is not necessary to use all the space.

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QUESTION  
NUMBER

1.(a)

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1.(b)

2.



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QUESTION  
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3.

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QUESTION  
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5.(a)

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5.(b)

6.



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7.

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8.



\* X 7 4 7 7 6 0 1 0 5 \*

QUESTION  
NUMBER

9.(a)

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9.(b)  
(i)

9.(b)  
(ii)



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QUESTION  
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10.(a)

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QUESTION  
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10.(b)

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QUESTION  
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11.

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12.



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QUESTION  
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13.

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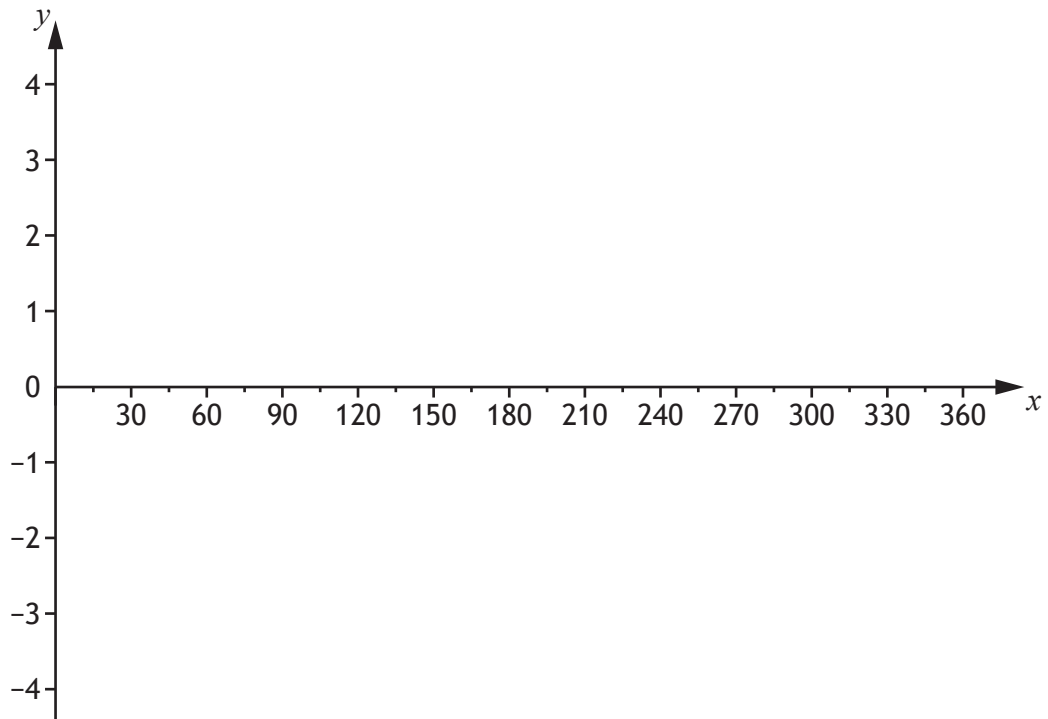
14.(a)



\* X 7 4 7 7 6 0 1 1 0 \*

14.(b)

An additional diagram, if required, can be found on Page 13.



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QUESTION  
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15.(a)

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15.(b)

15.(c)



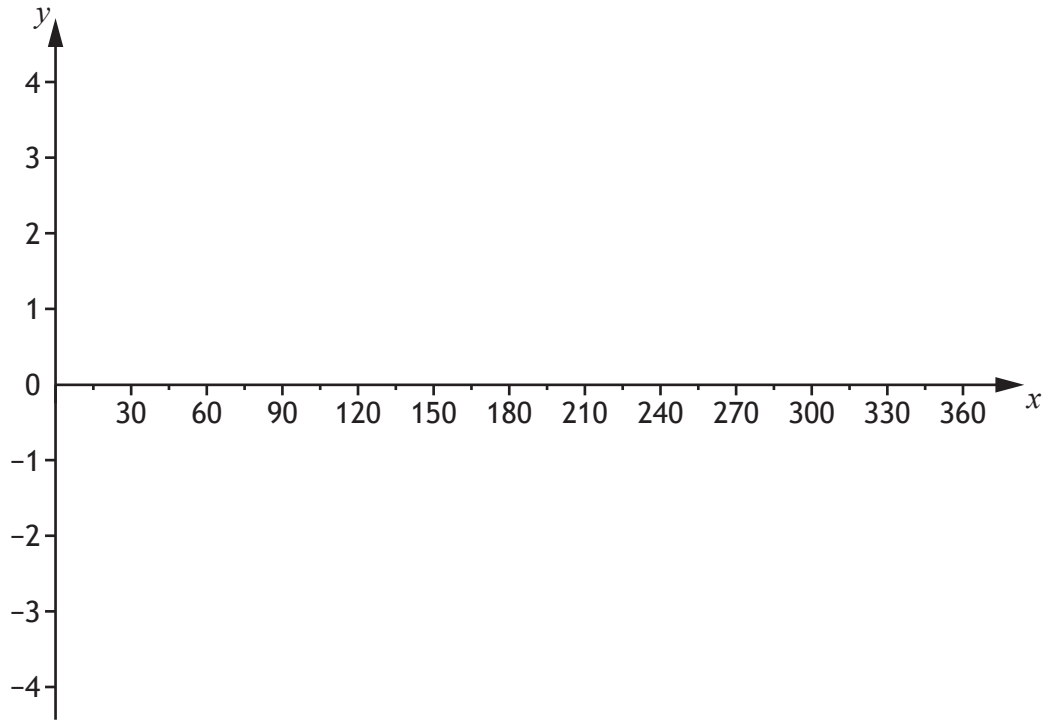
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QUESTION  
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ADDITIONAL SPACE FOR ANSWERS

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Additional diagram for Question 14(b).





QUESTION  
NUMBER

## ADDITIONAL SPACE FOR ANSWERS

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QUESTION  
NUMBER

ADDITIONAL SPACE FOR ANSWERS

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